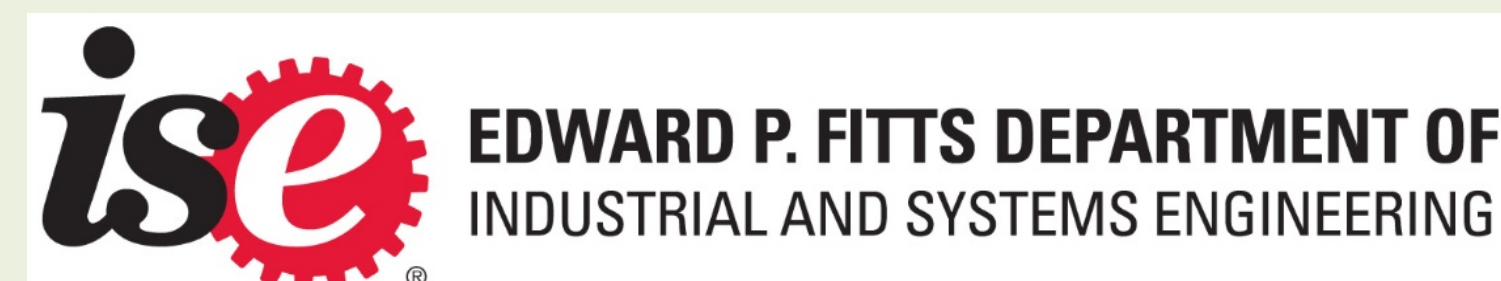


# IMPROVED FEATURE SELECTION WITH SIMULATION OPTIMIZATION

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## Why not include all features in the model?

- Overfitting
- Computationally expensive
- Less inference or interpretation power

## Research Methodology

Given a learning model (linear regression, random forest, etc.) we look for the best subset of features

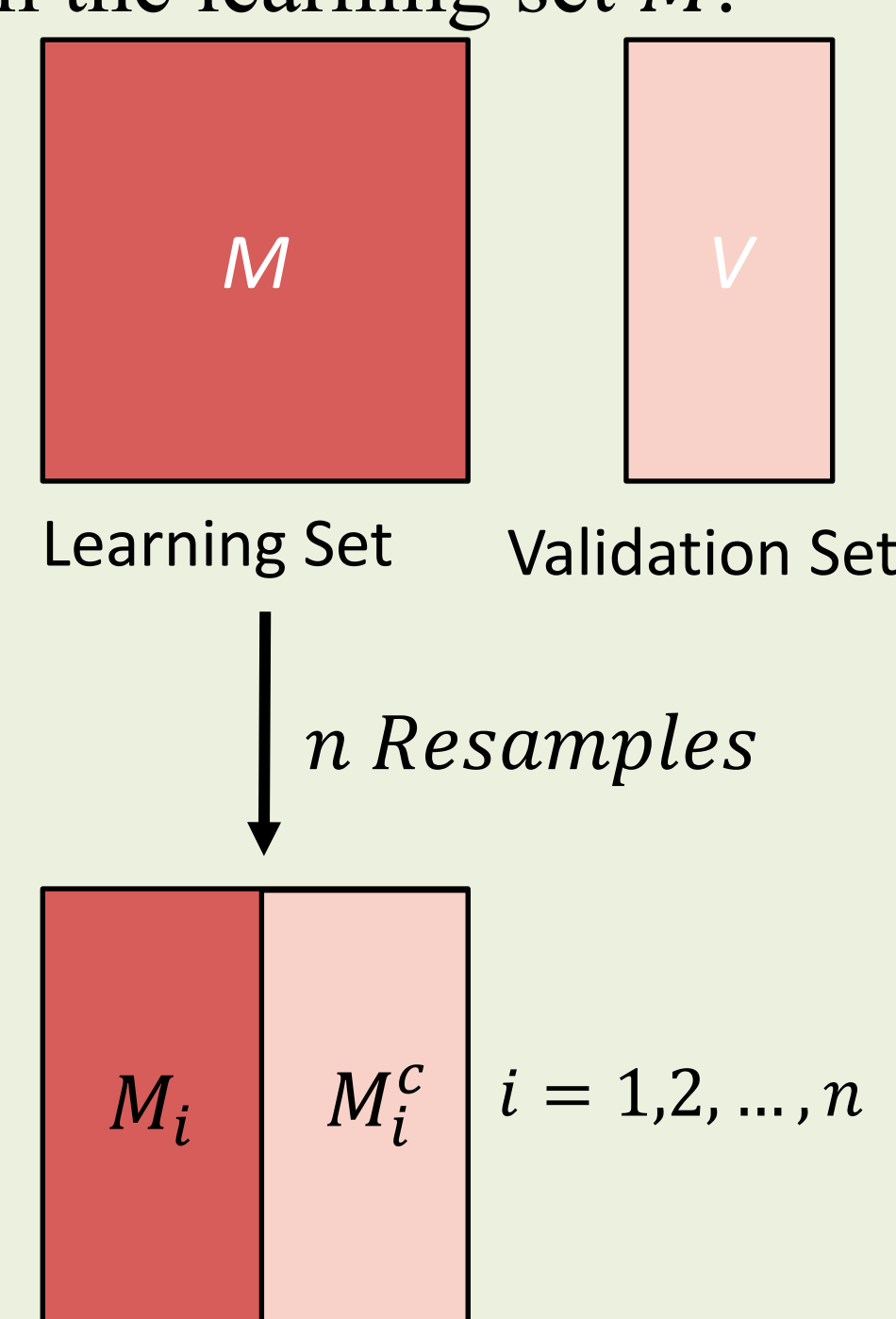
$$S^* = \operatorname{argmin}_S \sum_{j \in V} (f_{M,A,S}(x_j) - y_j)^2$$

where  $f_{M,A,S}(x_j)$  is the prediction model trained by the subset  $S$  of features of the learning set  $M$  with the learning algorithm  $A$ .

Estimate with its Sample Average Approximation

$$\hat{S}^* = \operatorname{argmin}_S \frac{1}{n} \sum_{i=1}^n \sum_{j \in M_i^c} (f_{M_i,A,S}(x_j) - y_j)^2$$

where  $M_i$  and  $M_i^c$  are resampled training and test sets within the learning set  $M$ .



## Experiment

We compare the performance of Simulation Optimization based Feature Selection SOFS with Genetic Algorithms as the optimization method

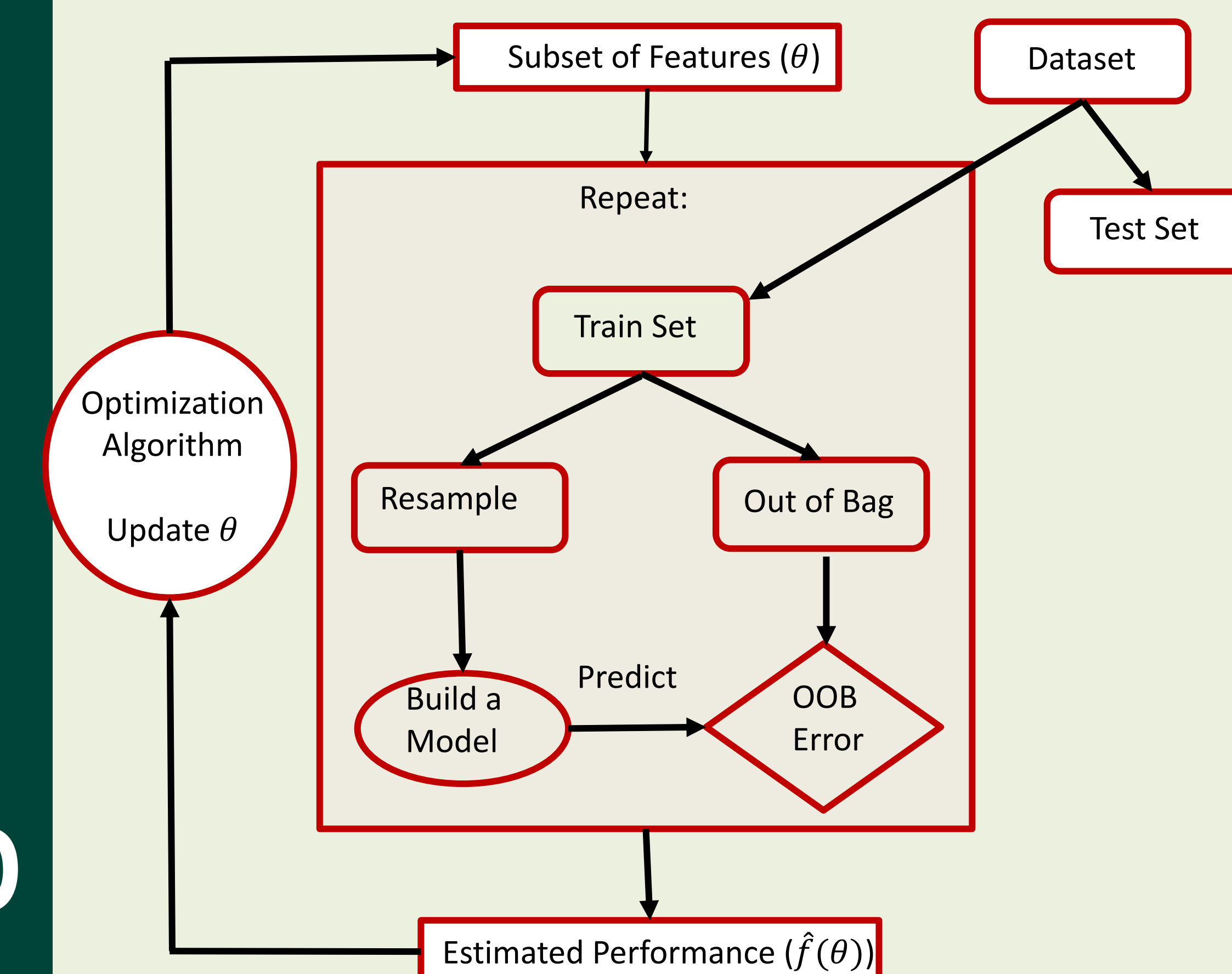
- in terms of mean absolute and squared error;
- with that of *Recursive Feature Elimination (RFE)*, the commonly used greedy approach that looks for the best subset size

$$d^* = \operatorname{argmin}_d \frac{1}{n} \sum_{i=1}^n \sum_{j \in M_i^c} (f_{M_i,A,d}(x_j) - y_j)^2;$$

- on a sample dataset from UCI repository with 55 features and 226 observations;
- on a two learning algorithms: linear regression (LM), and random forest (RF).

When looking in a dataset with many features for the most informative ones, we can develop an optimization problem that estimates the predictive accuracy of a prediction model with any subset of features by mimicking a simulation of the system under consideration, for which we only have the available data, through resampled datasets.

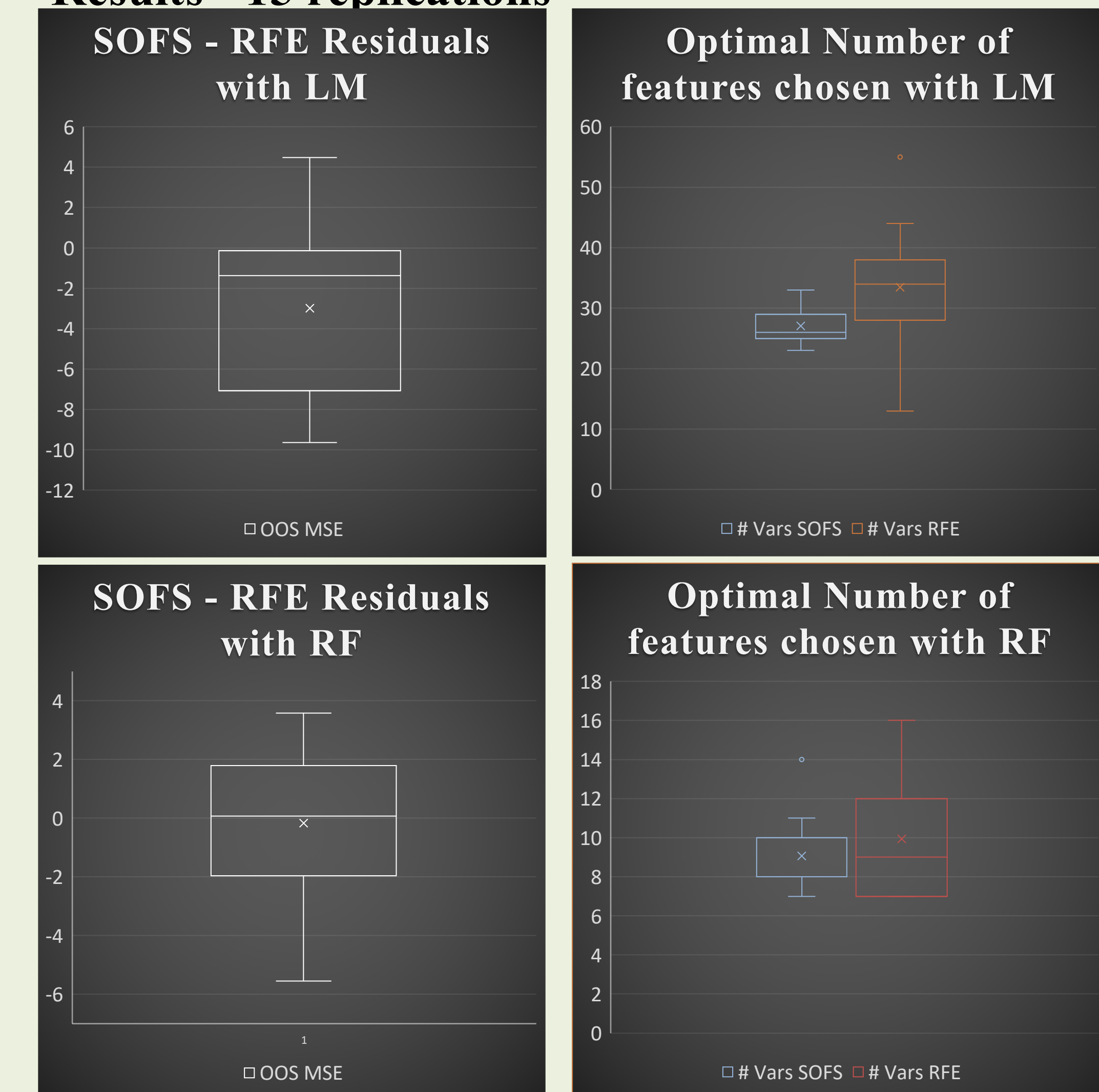
## Schematic Framework of SOFS



## Results - One replication

	RFE vs. SOFS	# Feat	IS MAE	OS MAE	IS MSE	OS MSE	Time
LM	RFE	33	2.44	3.45	11.92	22.56	.
	GA	27	2.38	3.17	11.62	19.58	.
RF	RFE	10	2.87	3.49	15.15	22.15	0.30
	GA	9	2.79	3.44	14.35	21.98	1015.56

## Results - 15 replications



## Conclusion

- SOFS gains higher accuracy in predictions and more precision in number of features for both LM and RF.
- The optimization routine GA is only run for a limited budget so in RF it can stop before convergence. More efficient optimization routines are under study.

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